# Shear Strength and Behavior of High Strength Reinforced Concrete Beams without Stirrups

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#### ABSTACT

This paper presents test results of twelve high strength reinforced concrete (HSRC) beams without stirrups which were tested to failure to investigate shear strength and behavior of (HSRC) beams without stirrups. The shear behavior, ultimate load-carrying capacity, and mode of failure are presented. The applicability the ACI 318M-11, Modified Zsutty, and Sudheer et al. equations are discussed. Moreover, the influences of shear span to effective depth ratio (a/d) and compressive strength  $(f_c)$  on shear strength and behavior of (HSRC) beams without stirrups are also discussed. It was found that, In general, with increasing each of compressive strength and (a/d) ratio the failure loads and consequently the shear strength of the beams decreased or didn't increase significantly. It was also found that ACI 318 M-11 overestimates for some test results (unsafe) while Sudheer et al underestimates for all test results equation excessively. However, Modified Zsutty equation underestimates the tested values for all the tested and could estimate shear capacity beams satisfactorily within a reasonable factor of safety.

Finally, a regression equation was proposed and it was found to be more reliable and safe in predicting shear strength of high strength reinforced concrete beams.

## **1. Introduction**

High-strength concrete is defined as having a specified compressive strength of 40MPa<sup>[1]</sup>. The use of High Strength Concrete is likely to increase further in 21<sup>st</sup> century with the construction of more high-rise buildings, long span pre-stressed bridges, and pre-cast elements in concrete structures. Concrete unlike steel is relatively non-homogenous material; hence its different structural properties are likely to change with increase in compressive strength. The high strength concrete is comparatively a brittle material as the sound matrix of aggregates and cement paste provides a smoother shear failure plane, which leads to its abrupt failure. Consequently the shear strength of high strength concrete does not increase in the same way, as its compressive strength. On the other hand, the availability of limited experimental work on the

high strength concrete makes it difficult to safely predict the shear capacity of reinforced concrete members which is presently evaluated on the basis of empirical equations proposed by different international building codes with certain modifications in the equations for normal strength concrete. As most of these equations have been derived on the basis of experimental data of concrete with compressive strength of 40MPa or less, therefore their application to higher values of compressive strength always raise questions in the minds of researchers. To further rationalize and generalize of these empirical equations for shear design of high strength reinforced concrete members, extensive research is required<sup>[2]</sup>.

## 2. Thesis Objectives

- To evaluate the shear strength of high strength reinforced concrete (HSRC) beams without web reinforcement.
- 2. To study the effects of various variables (a/d ratio and compressive strength  $f_c'$ ) on the shear strength of high-strength reinforced concrete beams without stirrups under a concentrated load.
- 3. To study the effects of various variables (a/d ratio and compressive strength  $f_c$ ') on the behavior of high-strength reinforced concrete beams without stirrups under a concentrated load.
- 4. To compare the ultimate diagonal cracking shear strength obtained from test results with values calculated from ACI and other researcher's predictions in order to obtain some conclusions that may help in the design of such members.

5. To obtain a formula to predict the shear strength of high-strength reinforced concrete beams and comparing with other researchers' data.

### **3. Experimental Program**

In this work twelve high strength reinforced concrete beams without stirrups were cast and tested under a single central concentrated load. The beam specimens were divided into three series according to their compressive strength and a/d ratio (shear span to effective depth ratio). Each series comprised of four beams as shown in Table 1.

| Table 1 | Series | Classifications | and Details |  |
|---------|--------|-----------------|-------------|--|
|         |        |                 |             |  |
|         |        |                 |             |  |

| Series<br>ID | Beam ID   | (a/d)   | fc'(MPa) |
|--------------|---|---|----------|
|              | B1S1  | 2.43  | 74.58    |
| <b>S</b> 1   | B2S1  | 2.86  | 74.58    |
| 51           | B3S1  | 3.29  | 74.58    |
|              | B4S1  | 3.71  | 74.58    |
|              | B1S2  | 2.43  | 67.72    |
| <b>S</b> 2   | Beam ID         (a/d)         formalization           B1S1         2.43         1           B2S1         2.86         1           B3S1         3.29         1           B4S1         3.71         1           B1S2         2.43         1           B1S2         2.43         1           B1S2         2.43         1           B1S2         2.86         1           B3S2         3.29         1           B1S3         2.43         1           B1S3         2.43         1           B1S3         2.43         1           B1S3         2.43         1           B1S3         3.71         1           B1S3         3.71         1 | 67.72   |          |
| 52           | B3S2  | 3.29  | 67.72    |
|              | B4S2  | 3.71  | 67.72    |
|              | B1S3  | 2.43  | 63.98    |
| <b>S</b> 3   | B2S3  | 2.86  | 63.98    |
| ~~           | B3S3  | 3.29  | 63.98    |
|              | B4S3  | D       (a/d)         2.43       2.86         3.29       3.71         2.43       2.86         3.29       3.71         2.43       2.86         3.29       3.71         2.43       2.86         3.29       3.71         2.43       2.86         3.29       3.71         2.43       2.86         3.29       3.71 | 63.98    |

### 4. Materials

<u>Cement</u> Ordinary local Portland cement (Type I) made in Tasluja factory was used. All results are also compliant with ASTM C150<sup>[3]</sup>. <u>Silica Fume</u> For achieving desired compressive strength microsilica as a mineral admixture was used in the mix. The product was ordered and tested outside of the country which was compliant to ASTM1240-95<sup>[4]</sup>.

Fine Aggregate (sand) The sand used in this work has a grading conforms to ASTM C33<sup>[5]</sup>limits. Coarse Aggregate (Gravel) The gravel with maximum size 19mm for series (S1) and 12.5mm for series (S2,S3) was used. The aggregate grading conforms to limits of ASTM C33<sup>[5]</sup>Standard Concrete Specification for Aggregates. Water Tap drinking water was used throughout this experimental work for washing, mixing of materials well for curing of as as the concrete. Chemical Admixture (HRWR) Superplasticizers are used to make the concrete more workable. In this work a superpalsticizer which is commercially known as (Proplast PC260 EXTRA) has been used. Reinforcement Steel Rebar Deformed Turkish made steel bars with nominal diameter 20mm were used as flexural reinforcement. All bars have been placed in the tension face of beams to avoid failing in flexure.

#### **5. Mix Proportions**

Three types of concrete mixes were used for casting all beam specimens. The selected mixes and their properties are summarized in Table 2.

#### 6. Specimen Details

The beam specimens were divided into three series each of four beams according to their compressive strength and a/d ratio. The cross sectional dimension of all beams were same (200\*400) mm but the length were varied between (2.00 to 2.80)m to achieve different a/d ratio. For all beams the amount of flexural reinforcements (which consists of 3-20mm dia.) were kept constant and this reinforcement amount was selected to be in acceptance with **ACI318**<sup>[6]</sup> limits for minimum and maximum amounts of flexural reinforcement. Table 3 summarizes details of all beam specimens.

Silica Fume kg/m<sup>3</sup> Lit/(100kg cement) Cement kg/m Gravel kg/m<sup>3</sup> Water kg/m<sup>3</sup> W/cm<sup>\*</sup> ratio Sand kg/m<sup>3</sup> f<sub>c</sub>' (MPa) (HRWA) Mix No. 25 525 840 945 0.95 140 0.25 74.58 1 (4.7%) 42.84 2 510 685 1080 3 143.73 0.26 67.72 (8.4%) 22.5 1100 450 700 1.1 151.2 0.32 3 63.98 (5%)

 Table 2 Mix Proportions and Properties

W/cm = water cementitious material ratio

#### 7. Test Procedure

All beams were tested after 28 days age. The digital dial gauge for measuring mid span deflection was erected as shown in Fig.1. Also, the available electrical (LVDT)s for measuring web shear crack width were erected on both sides (left side and right side)of the beam as shown in Fig.2. All beam specimens were tested as simply supported loaded by a single concentrated load at mid span. After these steps, the application of load was started in 4kN increments. At each load increment mid span dial gauge readings for deflection and (LVDT)s readings for web shear crack width at both sides of the beams were recorded. Furthermore, at each load increment, position, load magnitude, and cracks which appeared were marked and recorded carefully and these procedures were continued until failure. In parallel, the compressive strength test were carried out on standard (150\*150\*150)mm cubes together with the beams according to BS1881-116<sup>[7]</sup>

| Sorios     | Room | Total  | Effective | b   | h       | d   | a    |      |      |          | f'                    |       |
|------------|------|--------|-----------|-----|---------|-----|------|------|------|----------|-----------------------|-------|
| ID         | ID   | length | length    | mm  | mm      | mm  | mm   | a/h* | a/d  | ρ**      | т <sub>с</sub><br>MDo |       |
|            |      | mm     | mm        |     |         |     |      |      |      |          | IVII a                |       |
| }<br> <br> | B1S1 | 2000   | 1700      |     |         |     |      | 850  | 2.13 | 2.43     | 0.013464              | 74.58 |
| S1         | B2S1 | 2400   | 2000      |     |         |     | 1000 | 2.50 | 2.86 | 0.013464 | 74.58                 |       |
|            | B3S1 | 2800   | 2300      |     |         |     | 1150 | 2.88 | 3.29 | 0.013464 | 74.58                 |       |
|            | B4S1 | 2800   | 2600      | 200 |         |     |      | 1300 | 3.25 | 3.71     | 0.013464              | 74.58 |
|            | B1S2 | 2000   | 1700      |     | 200 400 |     |      | 850  | 2.13 | 2.43     | 0.013464              | 67.72 |
| \$2        | B2S2 | 2400   | 2000      |     |         | 350 | 1000 | 2.50 | 2.86 | 0.013464 | 67.72                 |       |
| 52         | B3S2 | 2800   | 2300      |     |         |     | 1150 | 2.88 | 3.29 | 0.013464 | 67.72                 |       |
|            | B4S2 | 2800   | 2600      |     |         |     |      | 1300 | 3.25 | 3.71     | 0.013464              | 67.72 |
| ,<br> <br> | B1S3 | 2000   | 1700      |     |         |     | 850  | 2.13 | 2.43 | 0.013464 | 63.98                 |       |
| S3         | B2S3 | 2400   | 2000      |     |         |     | 1000 | 2.50 | 2.86 | 0.013464 | 63.98                 |       |
|            | B3S3 | 2800   | 2300      |     |         |     | 1150 | 2.88 | 3.29 | 0.013464 | 63.98                 |       |
|            | B4S3 | 2800   | 2600      |     |         |     | 1300 | 3.25 | 3.71 | 0.013464 | 63.98                 |       |

Table 3 Properties and Details of Tested Beams

\*All values of this column are greater than 2 which confirms that all beams are out of limits of deep beams as described in ACI 318<sup>[6]</sup>.

\*\*All values of this column are within the maximum and minimum limits as described in ACI318<sup>[6]</sup>.

to obtain the compressive strength value of each beam series. For each series of beams three cubes were tested. Moreover, splitting tensile test according to ASTM C496<sup>[8]</sup> was carried out on cylindrical (150\*300)mm specimens. For each series of beams three cylinders were tested and average values of ( $f_{sp}$ ) were recorded.



**Fig.1** Deflection Digital Dial Gauge at Mid Span of Beams.



Fig.2 LVDT Instruments and Their Location

# 8. Experimental Results and Discussions 8.1 Midspan Deflection

After plotting load - deflection diagram, it was found that, in general, for the specified concrete compressive strength ,mid span deflection decreased as (a/d) ratio decreased. See Fig.3 which is presented for beams in (Series 2) . However, for the specified value of (a/d) ratio and different compressive strength, deflections were almost similar. See Fig.4 which is presented for beams (B2S1, B2S2, B2S3). In summary, it can be concluded that in this work (a/d) ratio factor has a greater effect on mid span deflection of the tested beams rather than compressive strength factor because when the latter factor is considered, the amount of longitudinal flexural reinforcement which was kept constant for all beams plays a vital role on deflection of the beams for different values of compressive strengths.



Fig.3 Load Deflection Relationship (Series 2)



**Fig.4** Load Deflection Relationship (B2S1, B2S2, B2S3)

## 8.2 Mode of Failure

All the beams were failed in shear as shown in Fig. 5. In general, there are two modes of inclined cracking that were observed. In the first mode, the inclined (diagonal) crack was formed independent of flexural cracks, and is often referred to as a "web-shear crack". In the second mode, the inclined crack started as an extension of an already developed flexural crack, this is generally denoted "flexural-shear crack". After the cracks as developed and with increasing of applied load one of the following two failure modes were observed for each beam specimen:

a) Shear Compression Failure : After formation of the inclined crack (web shear crack or flexural shear crack) and with increasing of the applied load, the crack extended toward the point load and the support. After some stages, the concrete above the upper end of the inclined crack and at the point of application of the point load exhibited more cracks and subjected to crushing resulting in the "*shear compression failure*" of the beam. This mode of failure was seen in all tested beams except in (B4S3).

b) Shear Tension Failure : After formation of the inclined crack (web shear crack or flexural shear crack) and with increasing of the applied load, the crack extended toward the point load and the support. After some stages, some secondary cracks due to the dowel action of the longitudinal flexural reinforcement bars appeared at the lower end of the secondary crack. These cracks propagated backward along the longitudinal bars from the inclined crack to the support and caused loss of bond, splitting of the concrete, further propagation of the cracks, and an anchorage failure of the

longitudinal bars. This failure is called "*shear tension failure*", and it was observed in (B4S3).





Fig.5 Crack Patterns of Tested Beams

# 8.3 Web-Shear Crack Width

For measuring the web-shear crack width of the beam specimens, available (LVDT)s were fixed on right and left sides of each tested beam at the mid height of its depth as shown in Fig.2. Through the (LVDT)s readings, web-shear crack width of the concrete beams was measured progressively with the load increments. For illustrating the effects of varying (a/d) ratio and compressive strength (fc') on web-shear crack width, load versus web-shear crack width diagrams considering these two variables for each beam series and its individuals are plotted. For example, in Fig.6 load versus web shear crack width for beams in (series 1) is illustrated for a specific value of fc' (74.58MPa) and different a/d ratio, and in Fig.7 load versus web shear crack width for beams (B2S1, B2S2, B2S3) is illustrated for a specific value of a/d (2.86) and different fc'. It can be concluded that for a specific compressive strength (f<sub>c</sub>') and different (a/d) ratio, as much as

(a/d) ratio decreased, web-shear crack width of the concrete beams decreased. On the other hand, for a specific value of (a/d) ratio, beams with higher compressive strength ( $f_c$ '), exhibited larger web-shear crack width and more brittle behavior accompanied by brisker failure.



**Fig.6** Load Versus Web-Shear Crack Width Diagram (Series 1)



**Fig.7** Load Versus Web-Shear Crack Width Diagram (B2S1,B2S2,B2S3)

# 8.4 Failure Loads a-Effects of (a/d)

Failure loads versus (a/d) ratios for all beams of the three series are plotted in Fig. 8 to visualize how the (a/d) ratio affects failure loads. It can be seen that for a specified value of compressive strength ,variation of (a/d) ratio has a direct effect on failure loads of the tested beam such that with increasing (a/d) ratio failure loads decreased.



**Fig.8** Effect of (a/d) on Failure Load **b-Effects of (f**<sub>c</sub>')

All tested beams were failed in shear, and their failure loads were dependant mostly on the value of compressive strength. For different values of (a/d) ratios, the effect of variation of the compressive strength on the tested beams is illustrated in Fig.9. It can be concluded that, in general ,with increasing compressive strength the failure loads decreased. However, there is some irregularity in beams of series 2 (S2) which can be justified by the different properties of these beams due to the existence of larger amount of silica fume and superplasticizer in their concrete mixture. It was also observed that with increasing the compressive strength, the tested beams behaved in brittle manner which results in more brisker failure of them.



Fig.9 Effect of (fc') on Failure Loads

## 9. Comparing Test Results with Other Provisions

The following three common equations were used for the purpose of comparison of test results:

## ACI 318M-11 Equation for Shear Prediction<sup>[6]</sup>

For members subjected to shear and flexure only, ACI 318M-11 propose the following equation for predicting shear strength of reinforced concrete beams  $V_c = [0.16 (f_c')^{0.5} + 17 \rho (V_u d / M_u)]b_w d$ but  $\leq 0.29 (f_c')^{0.5} b_w d$  .....(1) where:  $V_c =$  Nominal shear strength provided by concrete, N  $f_c' =$  Compressive strength of concrete (N/mm<sup>2</sup>)  $\rho =$  Flexural reinforcement ratio As/ (b<sub>w</sub> d)

 $V_u$  = Factored shear force at the section considered, N  $M_u$  = Factored moment at the section considered, N.mm  $b_w$ , **d** = Web width, effective depth, mm

# Modified Zsutty Equation for Shear Prediction<sup>[9]</sup>

Wafa, et al proposed some modifications for Zsutty Equations to predict shear strength of high strength concrete beams at different (a/d) ratio. For limits of normal beams (a/d >2.5), the following equation was proposed:  $V_c$  = Nominal shear strength provided by concrete. N  $f_c'$  = Compressive strength of concrete (N/mm<sup>2</sup>)

 $\rho$  = Flexural main reinforcement ratio [As/ (b<sub>w</sub> d)] a = Shear span, mm

 $\mathbf{b}_{\mathbf{w}}$ ,  $\mathbf{d}$  = Web width, effective depth, mm

# <u>The Equation Proposed by Sudheer et al. for</u> <u>Shear Prediction<sup>[10]</sup></u>

Sudheer et al, in 2010, proposed a linear regression equation in power series to estimate the shear resistance ( $V_c$ ) of high strength reinforced concrete beams as shown below:

 $V_c= 32 (f_t \rho / (a/d))^{0.8} b_w d$  .....(3) where

 $V_c$  = Nominal shear strength provided by concrete ,N ft = Tensile strength of concrete in (N/mm<sup>2</sup>).

 $\mathbf{a/d}$  = Shear span to effective depth ratio.

 $\rho$  = Flexural main reinforcement ratio [As/ (b<sub>w</sub>d)]

 $\mathbf{b}_{\mathbf{w}}$ , $\mathbf{d}$  = Web width, effective depth, mm

On the bases of test results  $(V_{test})$  and the predicted values  $(V_{predict})$  from each equations, the statistical parameters were calculated for the three beam series of the work as shown in Table 4.

# **10. Proposed Regression Equation for predicting Shear Strength of Beams Without Stirrups**

On the bases of the test results of the twelve reinforced concrete beams of this study, a regression analysis is performed to formulate a predictive equation for the ultimate shear strength of high strength reinforced concrete beams without stirrups. The equation is as follows:

 $V_{c} = 1.378 (f_{c}' \rho / \{ f_{t} (a/d)^{2} \} + f_{t} / (a/d) )^{1.393} b_{w} d$ .....(4)

 $V_c$  = Nominal shear strength provided by concrete, N  $\rho$  = Flexural main reinforcement ratio

| Series R           | Room   | f ' MDa      | a/d          | $V_{(predict)} / V_{(test)}$ |                 |         |  |  |
|--------------------|--------|--------------|--------------|------------------------------|-----------------|---------|--|--|
| Series             | Dealli |              | Iu u/u       | ACI                          | Modified Zsutty | Sudheer |  |  |
|                    | B1S1   | ÷            | 2.43         | 0.59                         | 0.57            | 0.58    |  |  |
| 1                  | B2S1   | 71 59        | 2.86         | 0.81                         | 0.74            | 0.69    |  |  |
| 1                  | B3S1   | 74.30        | 3.29         | 1.08                         | 0.96            | 0.84    |  |  |
|                    | B4S1   |              | 3.71         | 1.11                         | 0.94            | 0.77    |  |  |
|                    |        | 1            | Mean         | 0.8955                       | 0.8018          | 0.7205  |  |  |
|                    |        | Standa       | rd Deviation | 0.2468                       | 0.1807          | 0.1118  |  |  |
|                    | Со     | efficient of | Variation %  | 27.5634                      | 22.5366         | 15.5132 |  |  |
|                    | B1S2   |              | 2.43         | 0.47                         | 0.46            | 0.45    |  |  |
| 2                  | B2S2   | 67.72        | 2.86         | 0.80                         | 0.74            | 0.67    |  |  |
| -                  | B3S2   |              | 3.29         | 0.97                         | 0.86            | 0.73    |  |  |
|                    | B4S2   |              | 3.71         | 0.86                         | 0.73            | 0.59    |  |  |
| •                  |        | å            | Mean         | 0.7726                       | 0.6993          | 0.6102  |  |  |
| Standard Deviation |        |              |              | 0.2134                       | 0.1680          | 0.1200  |  |  |
|                    | Со     | efficient of | Variation %  | 27.6236                      | 24.0245         | 19.6720 |  |  |
|                    | B1S3   |              | 2.43         | 0.44                         | 0.43            | 0.43    |  |  |
| 3                  | B2S3   | 63 98        | 2.86         | 0.61                         | 0.57            | 0.52    |  |  |
| 5                  | B3S3   | 03.98        | 3.29         | 0.69                         | 0.62            | 0.54    |  |  |
|                    | B4S3   |              | 3.71         | 0.96                         | 0.83            | 0.67    |  |  |
|                    | Mean   |              | 0.6746       | 0.6117                       | 0.5414          |         |  |  |
| Standard Deviation |        | 0.2185       | 0.1634       | 0.1006                       |                 |         |  |  |
|                    | Co     | efficient of | Variation %  | 32.3913                      | 26.7164         | 18.5760 |  |  |

Table 4 Summary of Statistical Parameters of the Selected Equations Based on Test Results

 $f_c'$  = Compressive strength of concrete (N/mm<sup>2</sup>) a/d = Shear span to effective depth ratio  $f_t$  = Tensile strength of concrete in (N/mm<sup>2</sup>)  $b_w d$  = Web width, effective depth, mm

Table 5 presents the predicted results of the tested beams on the bases of Eq. (4) and comparison between predicted and test results.

# 11. Comparing The Proposed and Other Equations Based On the Other Researchers' Data

The proposed and other mentioned equations are applied on the data of the twelve tested beams of this study and the data of other 121 tested beams selected from other researchers' investigations. The compressive strength of the selected beams are between 41.45 MPa  $\leq f_c \leq 97.70$  MPa and (a/d) ratio are between 2.43 $\leq$  (a/d)  $\leq$ 6. Summary of the results of the calculated statistical parameters is summarized in Table6.

| Somiog   | Sarias Baam | f <sub>sp</sub> ' | f <sub>c</sub> ' | f <sub>c</sub> ' ρ d b <sub>w</sub> a/ | d                   | b <sub>w</sub> | o/d                        | V <sub>c</sub> (prop.) | Vc         | V <sub>c</sub> (prop.)/ |        |      |        |     |      |      |        |        |      |
|----------|-------------|-------------------|------------------|--|---------------------|----------------|----------------------------|------------------------|------------|-------------------------|--------|------|--------|-----|------|------|--------|--------|------|
| Series   | Dealli      | MPa               | MPa              |  | a/u                 | Eq. (5-4)      | (Test)                     | V <sub>c</sub> (Test)  |            |                         |        |      |        |     |      |      |        |        |      |
|          | B1S1        |                   | 71 59            | 71 50                                  |                     |                |                            |                        | 2.43       | 214.17                  | 192    | 1.12 |        |     |      |      |        |        |      |
| 1        | B2S1        | 1 21              |                  |  |                     |                |                            | 2.86                   | 169.87     | 140                     | 1.21   |      |        |     |      |      |        |        |      |
| 1        | B3S1        | 4.21              | 74.30            |  |                     |                | 3.29                       | 3.29 139.27            | 104        | 1.34                    |        |      |        |     |      |      |        |        |      |
|          | B4S1        |                   |                  |  |                     |                | 3.71                       | 117.49                 | 102        | 1.15                    |        |      |        |     |      |      |        |        |      |
|          | B1S2        | 2.00              | 3.89 67.72       |  |                     |                | 2.43                       | 192.23                 | 230        | 0.84                    |        |      |        |     |      |      |        |        |      |
| 2        | B2S2        |                   |                  | 0 67 72                                | 80 67 77            | 67 72 0.01     | 0.013464                   | 350                    | 200        | 2.86                    | 152.42 | 136  | 1.12   |     |      |      |        |        |      |
| Δ        | B3S2        | 3.69              |                  | 0.013404                               | .013404 330 200 3.2 | 3.29           | 124.93                     | 112                    | 1.12       |                         |        |      |        |     |      |      |        |        |      |
|          | B4S2        |                   |                  |  |                     |                |                            |                        |            |                         |        |      |        |     |      |      | 3.71   | 105.38 | 126  |
|          | B1S3        | 2 90              | 2 80             |  |                     |                |                            | 2.43                   | 191.87     | 242                     | 0.79   |      |        |     |      |      |        |        |      |
| 2        | B2S3        |                   |                  | 2 20                                   | 2 200 62 00         | 62 00          | 62.08                      | 63.08                  | 2 20 62 02 | 2 08                    |        |      |        |     |      | 2.86 | 152.18 | 174    | 0.87 |
| 5        | B3S3        | 5.69              | 03.90            |  |                     |                |                            |                        |            |                         |        | 3.29 | 124.76 | 152 | 0.82 |      |        |        |      |
|          | B4S3        |                   |                  |  |                     |                |                            | 3.71                   | 105.25     | 110                     | 0.96   |      |        |     |      |      |        |        |      |
| <b>.</b> |             | i                 | i                |  | i                   | <u>.</u>       | •                          | Mean                   | L          | 1.0144                  |        |      |        |     |      |      |        |        |      |
|          |             |                   |                  |  |                     |                | Sta                        | ndard Devia            | tion       | 0.1831                  |        |      |        |     |      |      |        |        |      |
|          |             |                   |                  |  |                     |                | Coefficient of Variation % |                        |            | 18.0476                 |        |      |        |     |      |      |        |        |      |

Table 5 Test and Predicted Shear Results Based on the Proposed Eq.(4)

**Table 6** Summary of Statistical Parameters for the Proposed and other Equations Based on

 the Current Test and other Researchers' Test Results

| Equation                  | No.of<br>Beams | Mean<br>V <sub>predict</sub> /<br>V <sub>Test</sub> | Standard<br>Deviation | Coeffficient<br>of Variation<br>% | Note                              |
|---------------------------|----------------|---|-----------------------|-----------------------------------|-----------------------------------|
| Proposed<br>Equation(5.4) | 133            | 0.8497  | 0.2773                | 32.6360                           | Overestimates for <b>40</b> beams |
| ACI 318M-11               |                | 1.0118  | 0.2504                | 24.7535                           | Overestimates for <b>74</b> beams |
| Modified Zsutty           |                | 0.8840  | 0.1893                | 21.4189                           | Overestimates for <b>35</b> beams |
| Sudheer<br>Reddy.L et al. |                | 0.8308  | 0.3343                | 40.2453                           | Overestimates for <b>43</b> beams |

#### **12.** Conclusions

Based on the results and the theoretical analysis of the twelve tested beams of this study and 121 beams from other researchers' data, and by taking into account the effects of (a/d) ratio and compressive strength on shear strength and behavior of high strength reinforced concrete beams without stirrups, the following conclusions could be drawn:

**1.**High-strength reinforced concrete beams without web reinforcement presented a very fragile behavior. The higher the concrete compressive strength is, the brisker the failure will be (more brittle behavior).

2. Both (a/d) ratio and compressive strength affect the mid span deflection and first flexural crack loads of the tested beams. However, (a/d) ratio factor has a more direct and regular effect rather than compressive strength factor because when the latter factor is considered, other factors such as the amount of longitudinal flexural reinforcement (which was kept constant for all beams in this study) and the different properties of the concrete mixtures due to existence of different contents of silica fume and superplasticizer also play vital roles on the deflection and consequently the first flexural load of the beams for different values of compressive strength.

**3.** In general, with increasing each of compressive strength and (a/d) ratio, the failure loads and consequently the shear strength of the tested beams decreased or in best case didnot increase significantly.

**4.** For a specific value of compressive strength (fc') and different (a/d) ratio, as much as (a/d) ratio decreased, web-shear crack width of the concrete beams decreased. Meanwhile, for a specific value of

(a/d) ratio, beams with higher compressive strength (fc'), exhibited larger web-shear crack width and more brittle behavior accompanied by brisker failure.

**5.** On the bases of results of this study, for each one of ACI 318M-11, Modified Zsutty, and Sudheer et al equations as much as the compressive strength and (a/d) ratio increased, the values of the (V(predict) / V(test)) also increased which indicates that the equations become less conservative.

**6.** ACI 318M-11 equation underestimates the tested values for almost all the tested beams which means that this equation is slightly conservative for the tested beams, and with increasing compressive strength and (a/d) ratio, it loses its conservation.

**7.** Modified Zsutty equation underestimates the tested values for all the tested beams and could estimate shear capacity satisfactorily within a reasonable factor of safety.

**8.** Sudheer et al equation underestimates excessively the tested values for all the tested beams and provides excessive factor of safety for the values.

**9.** Neither the three selected equations [ACI 318M-11, Modified Zsutty, and Sudheer et al ), nor the current proposed equation (Eq.4) are totally conservative for all the beams tested by other researchers in predicting the shear capacity of reinforced high strength concrete beams.

**10.** Both Modified Zsutty and the proposed (Eq.4) equations could estimate the shear strength of reinforced concrete beams of other researchers more accurately and safely comparing to other equations because they overestimated for fewer number of beams.

**11.** ACI 318M-11 equation has lower degree of safety and accuracy in predicting the shear capacity

of reinforced high strength concrete beams of other researchers comparing to other equations.

**12.** Even though Sudheer et al equation is excessively conservative on the bases of test results of this study, it could not predict the shear strength results of the other researchers safely and overestimates for larger number of beams comparing to modified Zsutty and the proposed (Eq.4) equations.

# 13. Notations

**a:** Shear span (Distance from concentrated load and center of the support), mm

a/d: Shear span to effective depth ratio

 $\mathbf{b}_{\mathbf{w}}$ : Beam width, mm

COV: Coefficient of variation

d: Effective depth ,mm

 $\mathbf{f}_{c}$ ': Cylindrical compressive strength of concrete, MPa

 $f_{cu}$ : Cubic compressive strength of concrete, MPa

 $\mathbf{f}_{sp}$ : Splitting tensile strength of concrete

 $\mathbf{f}_t$ : Tensile strength of concrete, MPa.

 $\mathbf{f}_{\mathbf{y}}$ : Yield strength of longitudinal reinforcement, MPa

 $\mathbf{f}_{yy}$ : Yield strength of shear reinforcement, MPa

 $\mathbf{f}_u$ : Ultimate strength of longitudinal reinforcement, MPa

h: overall depth of beam, mm

HSC : High strength concrete

HSRC : High strength reinforced concrete

HRWA: High range water reducing admixture

L: Length of beam, mm

Mu: Factored moment at critical section, N.mm

NSC : Normal strength concrete

**ρ:** Longitudinal tensile reinforcement ratio

 $\rho_v$ : Shear reinforcement ratio

RC: Reinforced concrete

S: Spacing between stirrups

 $V_c$ : Shear strength provided by concrete, N

 $v_{\rm cr}$ : Shear stress at cracking load, MPa

 $v_{\rm u}$ : Shear strength of concrete, MPa

Vu: Factored shear force at critical section, N

w/cm : Water - cementitious material ratio

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# المستخلص

معظم المعادلات التى تستخدم لحد الان لتخمين مقاومة القص( Shear Strength ) للعتبات الخرسانية المسلحة عالية المقاومة هي حصيلة تلك الا بحاث التى استخدمت فيها خرسانة بمقاومة انضغاط( Compressive Strength ) (40MPa ) او اقل, لذلك السبب, استخدام تلك المعادلات لتخمين قوة القص للعتبات الخرسانية ذات مقاومة انضغاط عالية ادت الى اسئلة كثيرة لدى الباحثين, لأن أى زيادة فى مقاومة الأنضغاط لا يؤدى الى زيادة واضحة فى مقاومة القص ( وفى معظم الأحيان تقل ) مقارنة مع الزيادة التى نجدها فى العتبات ذات مقاومة انضغاط

الأبحاث التى أجربت على العتبسات الخرسسانية المسلحة عاليسة القاومة, كل هذه الأمور ادت الي جدل كثير بين الباحثين وهذا ادي الى ضرورة استمرار الابحاث. هذا البحث محاولة جديدة لدراسة مقاومة القص ومعرفة سلوك العتبات الخرسانية المسلحة عاليسة المقاومة بدون (Stirrups), ومقاربة النتائج سبعض المعادلات الموجودة و ا يحاد معادلة عملية لتخمين مقاومة القص. ولهذا الغرض تم صب واختبسار ١٢ عتبسة خرسسانية مسلحة عاليسة المقاومية سيدون (Stirrups) بأنعساد ٢٠٠ مليم \* ٠٠٠ مليم وبأطوال مختلفة وبأخذ (a/d) (نسبة مسافة القص الى العمق الفعال للعتبات ) و مقاومة انضغاط ( Compressive Strength ) كمتغيرين اساسيين. علما ان (a/d) تضمنت القيم الاتية (٢.٧١, ٢.٢٩, ٣.٧٦) و مقاومة انضغاط تضمنت هذه القيم (63.98MPa, 67.72MPa, 74.58MPa). وقد تم اختبار جميع العتبات بوضع حمل في وسط كل عتبة وقرأة الانحراف في وسط العتبة ( Mid Span Deflection ) ثم قراءة سمك الشقوق في الاسطح الخارجية للعتبة ( Web Shear Crack Width). وقد اضهرت النتائج ان تأثير (a/d) اكثر انتظاما و فاعلية على مقدار الانحراف في وسط العتبات وعلى مقدار القوة اللازمة لضهور الشقوق الاولية( First Flexural Crack Load ) مقارنة بتأثير مقاومة ا انضغاط. وقد اضهرت النتائج ايضا ان بزيادة مقاومة انضغاط و (a/d) القوة اللازمية للانهيسار (Failure Load) ومقاومية القص( Shear Strength ) تقل او لا تزيد بنسبة واضعة. وبعد مقارنة نتائج الاختبار بالمعادلات الموجودة تبين ان المعادلية ( ACI 318M -11 ) تعطى نتائج اعلى من نتائج الاختيار

لەسەر كۆنكريّتى بەرگرى بەرز كراوە لەم بوارەدا بوونەتــه هــۆى مشت ومر و پيويست بوونى بەردەوامى تويزثينــەوە ئــهم بــوارەدا . ئەم توێژينەوەيە ھەوٽێكە بـۆ ٽێكۆٽينـەوە ئـه ھەٽسـوكەوت و توانای بهرگهگرتنی برین نه رایهنی شیشداری دروست کراو نه كۆنكريتى بەرگرى بەرز بە بى بوونى شيشى برين ( Stirrups ) پاشــان بــهراورد كردنــى ئه نجامــهكان بــه هەنــدێك لــهو هاوكيْشانەى كە ھەن وە ھەروەھا دارشتنى ھاوكيْشەيەكى نـويْى گونجاوتر بۆ خەملاندنى تواناى بەرگەگرتنى برين لـه رايـەنى شیشداری دروست کراو نه کونکریتی بهرگری بهرز به بی بوونی شیشی برین ( Stirrups ). بۆ ئەو مەبەستە, دوازدە دانە رايەنى شیشداری کۆنکریتی دروست کراو نه کونکریتی بهرگری بهرز به بی شیشی ( Stirrups ) به قهبارهی ( ۲۰۰ \*۲۰۰ ملم ) و به دریدژی جیاواز دروست کران و یاشان خرانه ژیّر تاقی کردنهوهوه به رهچاوگرتنی ههریهك له ریّژهی ( a/d ) ( رِیْژهی دووری بـرین بـوّ قولی کارا ) و توانای بهرگهگرتنی کونکریّت( Compressive Strength ) وەك دوو گۆړاوى سەرەكى ئىكۆڭىنەوەكە. چوار نرخ بوز ريْـرْهى ( a/d ) بـهكارهات كـه بريتـى بـوون لـه ( ۲.٤٣, ۲.٨٦, ۳.۲۹, ۳.۷۱ ) وه ههروهها سی نرخ بو توانای بهرگه گرتنی کۆنکریت که بریتی بوون نه ( 63.98, 67.72, 74.58 MPa ) بەكارھات. سەرجەم رايەڭەكان تاقى كردنــەوەيان بــۆ نه نجامدرا لهسهر دوو راگری ساده ( Simply Support ) له ژير کاريگەرى يەك ھيْـزدا ئــه ناوەراسـتى رايەللەكانــدا وە ئــه قۆناغه جياوازەكانى تاقى كردنەوەكاندا ولەگـەل زيـادكردنى هيْزدا,بوْ ههر رايه ٽيْك, بري دابهزيني ناوه راست ( Mid Span Deflection ) وه ههرومها زیاد بوونی ئهستوری درزهکانی سهر رووی رایه له کان ( Web Shear Crack Width ) ده پی ورا به ئاميْرى تاييهت. له ئه نجامي تاقى كردنهوهكهوه دەركهوت که گۆړاوی ( a/d ) کاریگهریهکهی راستهوخو ترو ریکخراو تره له گۆڕاوی توانای بهرگه گرتنی کۆنکریت ( Compressive Strength ) له سهر ههریهك له دابهزینی ناوهراست ( Span Deflection ) و ئــه و هيٽـزه کـه دهبيٽتـه هــوٚى

لبعض من النماذج وهذا يعنى انها معادلة غير امنة بينما معادلة ( Sudheer et al ) تعطى نتائج اقل بكثير من نتائج الاختبار Modified ( مبالغ فيها لكل النماذج. لكن معادلة ( Modified تعطى نتائج اقل من نتائج الاختبار لكل العتبات بفارق مقبول وهذه اشارة الى انها افضل معادلة لتخمين مقاومة بفارق مقبول وهذه اشارة الى انها افضل معادلة لتخمين مقاومة القص للعتبات مقارنة بمعادلات اخرى. واخيرا , تم استحداث معادلة جديدة بأستخدام نتائج الفحوص وبعد مقارنة هذه المادلة الجديدة بالمعادلات الاخرى باستخدام نتائج النماذج الحالية ونتائج ا بحاث سابقة تبين ان المادلة الجديدة موثوقة وامنة مقارنة بالمعادلات اخرى لتخمين مقاومة القص للعتبات الخرسانية الملحة عالية المقاومة بدون (Stirrups).

# پوخته

زۆربەى ئەو ھاوكێشانەى كە تا ئێستا بـ كاردێن بـۆ خەملاندنى برى بەرگەگرتنى برين ( Shear Strength ) كە رايه لی شیشداری دروست کراو نه کونکریتی بهرگری بهرز. زوربهیان داریژراون له سهر بنچینهی ئهو زانیاری و ئه نجامانهی که دهست کهوتوون له ئه نجامی تاقی کردنهوه لهسهر ئهو نمونه کۆنکریتیانهی که توانای بهرگه گرتنیان( Compressive Strength ) ( Strength ) يان كەمترە. كە بەر ئەم ھۆيە, بەكارھێنانى ئەم ھاوكێشانە بۆ كۆنكرێتى بەرگرى بەرزى زياتر له ( 40MPa ) بوهته جيّى پرسيار له لاى تويَّژهرانى ئهم بواره چونکه وەك دەركەوتووە ئەگەڭ زيادبوونى تواناى بەرگـەگرتنى كۆنكريّت( Compressive Strength), بەرگە گرتنى برين ( Shear Strength ) زیاد ناکات بهراورد بهو زیاد بوونهی که له كونكريتى ئاسايدا دەبينريت (تەنانەت كەميش دەكات). ئەمە جگە ئەوەى كە بوونى ژمارەيەكى زۆر ئەو ھۆكارانەى كە کاردهکهنه سهر توانای بهرگه گرتنی برین له رایه لی شیشداری كۆنكريْتيداو ھەروەھا كـەمى ژمـارەى ئـەو تويْژينەوانـەى كـە پهيدابوونی درزی يه کهمی چهمانهوه ( First Flexural Crack Load ). وه ههروهها دهرکهوت که به شیوه یه کی گشتی, زياد بووني هەريەك لـه لـه توانـاي بەرگـهگرتنى كۆنكريّت و ( a/d )) دەبيتە ھۆى كەمبونەوەى ھەربەك لەو ھيزەى كە دەبيتە هـوى تيكشـكانى رايه لهكه ( Failure Load ) و هـهرومها توانسای بهرگسه گرنسی بسرین (Shear Strength). هەروەها ياش بەراورد كردن دەركەوت كە ھەنىدىك ئە نىرخە خەملْيْنراودكانى ھاوكيْشەي ( ACI 318M -11 ) زياترن لەو ئه نجامانهی که دهست کهوتوون له تاقی کردنهوهکهوه(واته سەلامەت نيە ) كە ئەمەش پيۆويستە رەچاو بكريّت لـه كاتى بەكارھێنانى ئەم ھاوكێشەيە بۆكۆنكرێتى بەرگرى بەرز. بەڵام سەرجەم نرخە خەمليّنراوەكانى ھاوكيّشـەى ( Sudheer et al ) به حیاوازیهکی زوّر کهمترن نه ف نجامانه که دهست كەوتوون لە تاقى كردنەوەكەوە, ئەمە لە كاتېكىدا كـە ھـەموو نرخه خەملينز اوهکانی هاوکيشهی ( Modified Zsutty ) سه شيوه یه کی گو نجساوتر لسه هاوکیٰشسه کانی تسر کسه مترن لسه و ئه نجامانهی که دهست کهوتوون له تاقی کردنهوهکهوه که ئەمەش بەلگەي گونجاوتربونى ئەم ھاوكيشەيە دەردەخات لەوانى تر. له كۆتاييدا له سەر بنچينەي ئەو ئە نجامانــەي كــه دەست كەوتوون, ھاوكێشەيەكى نوى داريْـ ژراوە. ياش بـەراورد كردنى ئه نجامى تاقى كردنهومى ئهم تويْژينهوميهو هـهرومها ئـه نجامي تـاقي كردنـهوهكاني تويِّرژهرهواني تـر بـه نرخـه خەملىندراوەكانى بەرامبەريان بە بەكارھىنانى ھەرىبەك ئە هاوکیْشه نویْکه و سی هاوکیْشهکهی تر دەرکهوت که هاوکیْشه نویکه دهتوانیت به شیوه یه کی سه لامهت تر و گونجاوتر ئه نجامه کان بخه ملیّنیّت به راورد به هاوکیّشه کانی تر.